

Module 1: Devices
Diodes, MOS transistors, models

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Goal of this chapter

- Present intuitive understanding of device operation
- Introduction of basic device equations
- Introduction of models for manual analysis
- Introduction of models for SPICE simulation
- Analysis of secondary and deep-sub-micron effects
- Future trends

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Outline

- Semiconductor Physics
- The diode
 - Depletion, I-V relations, capacitance,
- The MOS transistor
 - First glance, threshold, I-V relations, models
 - Dynamic behavior (capacitances), resistances,
- Process variations

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Course Material for Devices

Chapter 3

P = primair, I = illustratie, O = overslaan

C	3.1	Introduction	74
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(1) Vervangend studiemateriaal voor dynamisch gedrag in syllabus

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Modeling

- An **abstraction** of (the properties) of something to help **understanding** and **predicting** its behavior
- **Domain Specific**: weather, climate, economy, stock market, ...
- Different models for something to **answer different questions**
- **Black-Box** modeling vs. **Physically Based**

■ After Einstein: a model should be as simple as possible, but not simpler

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Semiconductor Physics

- All electrical behavior is determined by underlying physics
- This course is not about the physics
- But some small amount of background information helps built intuition
- Intuition is what an engineer/designer needs most

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Periodic System

Legend

- Li Solid
- Cs Liquid
- Alkali metals
- Alkali earth metals
- Transition metals
- Rare earth metals
- Other metals
- Noble gases
- Halogens
- Other nonmetals
- Synthetic

<http://www.chemcool.com/>

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Periodic System

Name	Symbol	#	Valence
Silicon	Si	14	4
Boron	B	5	3
Phosphor	P	15	5
Arsenic	As	33	5
Germanium	Ge	32	4

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Semiconductor Physics

See also Tipler (BKV) 38.5

Intrinsic Si

- Ideal crystal structure
- Valence 4
- almost no free carriers
- almost no conduction

$[n] = [p] = n_i = 1,5 \cdot 10^{10} / cm^3$
at 300 K for silicon

- doping with valence 5 atoms (Phosphor, Arsenic) introduces "loose electrons"
- electron donor
- conductivity depends on doping level

$n \cdot p = n_i^2$ (in equilibrium)

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Semiconductor Physics

- doping with valence 5 atoms (Phosphor, Arsenic) introduces "loose electrons"
- electron donor
- conductivity depends on doping level

- doping with valence 3 atoms (Boron) introduces "loose holes"
- electron acceptors
- hole conductivity lower than electron conductivity

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Semiconductor Physics

Si in equilibrium : $n \cdot p = n_i^2 = 2,25 \times 10^{20}$ at 300K
Intrinsic *Si* : $n = p = n_i$

$N_D \gg N_A$	$N_A \gg N_D$
Electron donors: As, P n-type Si $n \approx N_D, p = n_i^2 / n$ Electrons: majority carriers Holes: minority carriers Resistive material Conductivity depends on N_D	Electron acceptors: B p-type Si $p \approx N_A, n = n_i^2 / p$ Holes: majority carriers Electrons: minority carriers Hole conductivity lower than electron conductivity

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The diode

- Depletion, I-V relations, capacitance,

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The diode: non-linear resistance

$I = \frac{V}{R}$

$R = \cotan(\alpha)$

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The Diode

See also Tipler (BKV) 38.6

Cross-section of pn-junction in an IC process

One-dimensional representation

Anode

Cathode

Diode symbol

Diode is abundant as MOS source/drain

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Ideal Diode, Abrupt pn junction Intuitive Description

Join n-Si with p-Si

Concentration gradient of free carriers

Diffusion current

Space charge (depletion) region

Electric field

Drift current opposite to diffusion

equilibrium

p-Si n-Si

Electron diffusion hole diffusion

hole drift Electron drift

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Depletion Region

(a) Current flow.

(b) Charge density.

(c) Electric field.

(d) Electrostatic potential.

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Conduction

Typical N_A, N_D : $10^{15} \dots 10^{17}/\text{cm}^3$, ϕ_0 around 0.6 V

Built-in Potential

$$\phi_0 = \phi_T \ln \left[\frac{N_A N_D}{n_i^2} \right]$$

Thermal voltage

$$\phi_T = \frac{kT}{q} = 26\text{mV at } 300\text{K}$$

By applying an external voltage, width of depletion region can be changed

- Forward: becomes smaller and smaller, finally conduction
- Reverse: becomes wider and wider => no conduction

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Diode Current

(a) On a linear scale

(b) On a logarithmic scale (forward bias)

$$I_D = I_S (e^{V_D/\phi_T} - 1)$$

- I_S : Saturation current
- Proportional to diode area
- Depends on doping levels, and widths of neutral regions
- Usually determined empirically

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Models for Manual Analysis

$I_D = I_S \left(e^{\frac{V_D}{\phi_T}} - 1 \right)$

(a) Ideal diode model

(b) First-order diode model

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Diode Model Example

$I_s = 0.5e^{-16} \text{ A}$
 $kT/q = 25 \text{ mV}$
 $V_s = 1.6 \text{ V}$
 $R_s = 1 \text{ k}\Omega$

Determine I_D

$I_D = I_S (e^{V_D/\phi_T} - 1)$ (diode model)
 $V_s - R_s I_D = V_D$ (Kirchof)
 $V_s - R_s I_S (e^{V_D/\phi_T} - 1) = V_D$ 😞

Iteration

start: $V_D = 1.0 \text{ V}$
 $\Rightarrow I_D = (V_s - V_D)/R_s = 0.600 \text{ mA}$
 $\Rightarrow V_D = \phi_T (1 + \ln(I_D/I_S)) = 0.663 \text{ V}$
 $\Rightarrow I_D = 0.937 \text{ mA}$
 $\Rightarrow V_D = 0.674 \text{ V}$
 $\Rightarrow I_D = 0.926 \text{ mA}$
 $\Rightarrow V_D = 0.674 \text{ V}$ 😊

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Diode Model Example

$I_s = 0.5e^{-16} \text{ A}$
 $kT/q = 25 \text{ mV}$
 $V_s = 1.6 \text{ V}$
 $R_s = 1 \text{ k}\Omega$

First order solution

$V_D = 0.6 \text{ V} \Rightarrow I_D = 1 \text{ mA}$ error = 8 %

Now, take $V_s = 10.6 \text{ V}$ $R_s = 10 \text{ k}\Omega$

The error will be

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Capacitance

$Q = CV$

$C = \tan \alpha$

$C = \epsilon \frac{A}{t}$

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Linearized Large-Signal Diode Capacitances

Summary:

- Diode capacitances highly non-linear
- Difficult with manual calculation
- We are ultimately interested in amount of charge being stored on (or removed from) capacitor
 - Since it takes time for this to happen, this determines the final switching speed of the circuit: more charge means more time!
- Linear capacitance: $\Delta Q = C\Delta V$: easy to work with
- Small-signal capacitance: $dQ = C_dV$: for analog appl.
- Non-linear capacitance: $\Delta Q = f(V_{low}, V_{high})$

Work with C_{eq} for standardized voltage swings

See the syllabus!

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Large Signal Equivalent Diode Capacitance

step voltage

$C_{eq} = f(V_{high}, V_{low})$

$= \frac{Q_f(V_{high}) - Q_f(V_{low})}{V_{high} - V_{low}}$

Linear C

$C = \tan \alpha$

Non-linear C

$C_{eq} = \tan \alpha'$

$\frac{dQ}{dV}$

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The MOS Transistor

- First glance, threshold, I-V relations, models
- Dynamic behavior (capacitances), resistances, more Second-Order effects, models

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The MOS Field Effect Transistor – compared to Storey

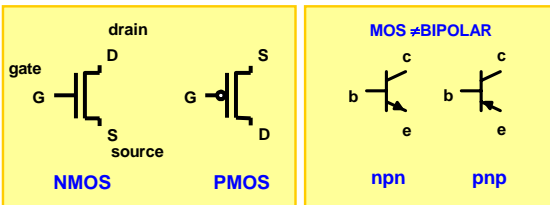
- MOSFET transistor is not a JFET
- Other operating regions compared to saturation region (linear, velocity saturation) also important
- Include more effects (channel length modulation)
- Short-channel devices
 - bad for some analog circuits,
 - good for (most) digital circuits
- We will develop understanding of basic device equations

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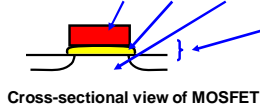
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MOSFET Transistors



MOSFET = "Metal"-Oxide-Semiconductor Field-Effect Transistor



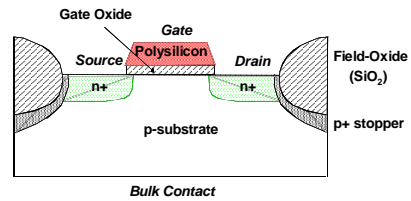
Gate (terminal of MOSFET) ≠ Logic gate

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The MOS Transistor



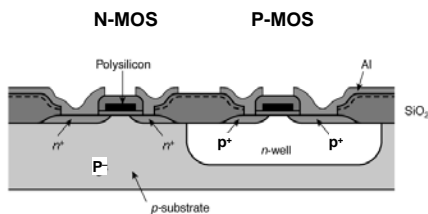
CROSS-SECTION of NMOS Transistor

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Cross-Section of CMOS Technology

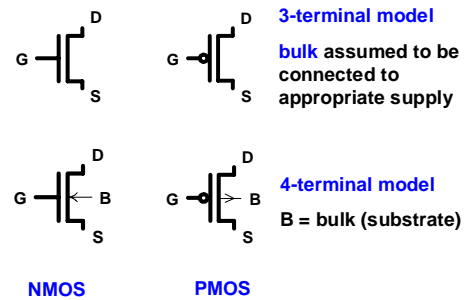


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MOS Transistors



NMOS

PMOS

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MOS Transistor Switch Level Models

NMOS

Simplest possible useful model

Position of switch depends on gate voltage

V_G	NMOS	PMOS
hi	closed	open
lo	open	closed

- Connection between source and drain depends on gate voltage, current can flow from source to drain and vice versa if closed
- No static current flows into gate terminal

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Mos Switch Model (2)

Position of switch depends on gate voltage		
V_G	NMOS	PMOS
hi	closed	open
lo	open	closed

A = 0 NMOS

(a) Open

A = 1 NMOS

(b) Closed

A = 1 PMOS

(a) Open

A = 0 PMOS

(b) Closed

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CMOS Inverter Operation Principle

inverter

equiv. ckt. with input 1

equiv. ckt. with input 0

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From Logic to Voltages

(a) Power supply connection

(b) Logic definitions

Ideal logic 0 corresponds to $V_x = 0V$
 Ideal logic 1 corresponds to $V_x = V_{DD}$

Not all actual voltages in circuit necessarily correspond to ideal logic levels, see figure (b) above

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From Logic to Voltages

Logic view

Voltage view

Note:

- GND = GROUND = 0V
- Sometimes also called V_{SS}
- V_{DD} is highest voltage level in circuit
- V_{DD} value depends on technology, has been reduced from 5V to 1V and lower over the years
- All voltages V_x in ckt: $0 \leq V_x \leq V_{DD}$

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Source and Drain Terminals

	NMOS	PMOS	PMOS
Source	Lowest potential	Highest potential	Lowest potential
Drain	Highest potential	Lowest potential	Highest potential

Note 1: Polarities of PMOS voltage reversed when compared to NMOS
 Note 2: MOS transistor is completely symmetrical! Can interchange source and drain, without any effect. Source/drain is only a naming convention.

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nFET Threshold Voltage (drempelspanning)

(a) Gate-source voltage

(b) Logic translation

nFET is off when $V_{GSn} \leq V_{Tn}$
nFET is on when $V_{GSn} > V_{Tn}$

$V_{Tn} \sim 0.5 \dots 0.7V$

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pFET Threshold Voltage

nFET is off when $V_{GSn} \leq V_{Tn}$
nFET is on when $V_{GSn} > V_{Tn}$

pFET and nFET behave complementary

Equivalent conditions

pFET is off when $V_{GSp} \geq V_{Tp}$
pFET is on when $V_{GSp} < V_{Tp}$

pFET is off when $-V_{GSp} \leq -V_{Tp}$
pFET is on when $-V_{GSp} > -V_{Tp}$

pFET is off when $|V_{GSp}| \leq |V_{Tp}|$
pFET is on when $|V_{GSp}| > |V_{Tp}|$

$V_{Tp} \sim -0.5 \dots -0.7V$ (negative!)

Often most useful

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Exercise

transistor on the left using

nFET is off when $V_{GSn} \leq V_{Tn}$
nFET is on when $V_{GSn} > V_{Tn}$

corresponds to diagram on right

Draw same diagram for PMOS using

pFET is off when $-V_{GSp} \leq -V_{Tp}$
pFET is on when $-V_{GSp} > -V_{Tp}$

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MOS Transistor Threshold Voltage

Threshold voltage V_T : point at which transistor turns on

Position of switch depends on gate voltage (relative to source)

V_{GS}	NMOS	PMOS
$V_{GS} > V_T$	closed	open
$V_{GS} < V_T$	open	closed

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Is this all there is?

- You don't believe that (CMOS) life can be so simple, do you?
- Think of some of the things that you would expect to be non-idealities of CMOS as a switch
- Discuss with your neighbor
- Share with us
- Since we want to design CMOS circuits, we need a deeper understanding of CMOS circuits
- Next slide shows where we are going

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MOS Models for Manual Analysis

determined by circuit
 V_{DS}, V_{GS}, V_{SB}

determined by technology
 $k, \lambda, V_{DSAT}, V_{TO}, \gamma, \phi_F$

MOS model for manual analysis

$I_D = k(V_{GT} V_{MIN} - 0.5V_{MIN}^2)(1 + \lambda V_{DS})$ for $V_{GT} \geq 0$
 $= 0$ for $V_{GT} \leq 0$

$V_{MIN} = \text{MIN}(V_{DS}, V_{GT}, V_{DSAT})$

$V_{GT} = V_{GS} - V_T, \quad V_T = V_{T0} + \gamma(\sqrt{|-2\phi_F + V_{SB}|} - \sqrt{-2\phi_F})$

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nMOS Transistor Operation

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Body Effect

- V_T is **not constant**
- Depends on V_S vs V_B
- Our wish is to understand & predict behavior of CMOS devices
- We will start with V_T

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MOSFET gate as capacitor

- Gate capacitance helps determine charge in channel which forms **inversion region**.
- Basic structure of gate is **parallel-plate capacitor**:

$$C_{ox} = \epsilon_{ox} / t_{ox}$$

$$\epsilon_{ox} = \epsilon_0 \epsilon_r$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

$$\epsilon_r = 3.9 \text{ (SiO}_2\text{)}$$

Note: [F] vs. [F/m²]

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The Threshold Voltage

$$V_T = \phi_{ms} - 2\phi_F - \frac{Q_B}{C_{ox}} - \frac{Q_{SS}}{C_{ox}} - \frac{Q_f}{C_{ox}}$$

Contact Potential
Fermi Potential
Depletion Layer Charge
Surface Charge
Implants

$$Q_B = \gamma(\sqrt{|-2\phi_F + V_{SB}|}) \quad \text{with} \quad \gamma = \frac{\sqrt{2q\epsilon_{Si}N_A}}{C_{ox}}$$

Body Effect Coefficient

Forget all this

$V_T = V_{T0} + \gamma(\sqrt{|-2\phi_F + V_{SB}|} - \sqrt{|-2\phi_F|})$
But be able to use this

with

$$V_{T0} = \phi_{ms} - 2\phi_F - \frac{Q_{B0}}{C_{ox}} - \frac{Q_{SS}}{C_{ox}} - \frac{Q_f}{C_{ox}}$$

and this

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$I_D(V_{GS}, V_{DS}, V_{BS})$

MOS model for manual analysis

$$I_D = k(V_{GT}V_{MIN} - 0.5V_{MIN}^2)(1 + \lambda V_{DS}) \quad \text{for } V_{GT} \geq 0$$

$$= 0 \quad \text{for } V_{GT} \leq 0$$

$V_{MIN} = \text{MIN}(V_{DS}, V_{GT}, V_{DSAT})$

- Different operation regions
- Different behavior for each region:
 - off
 - resistive
 - saturation
 - velocity saturation

← NEXT

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Current-Voltage Relations

MOS transistor and its bias conditions

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$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$ I-V In Resistive Region

$Q_i(x) = -C_{ox}[V_{GS} - V(x) - V_T]$ **Inversion Charge**

$I_D = -\mu_n \frac{dV}{dx} Q_i(x) W$ **I_D Drain Current**
 μ_n mobility (n-Si)

$\int_0^L I_D dx = -\mu_n \epsilon(x) = \mu_n \frac{dV}{dx} V dV$

$I_D L = \mu_n C_{ox} W \left[(V_{GS} - V_T) V - \frac{1}{2} V^2 \right]_0^{V_{DS}}$

$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$

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Process Gain and Device Gain

$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$

$k'_n = \mu_n C_{ox} = \mu_n \frac{\epsilon_{ox}}{t_{ox}}$ **Process transconductance parameter**

$k = k'_n \frac{W}{L}$ **Gain factor of device**

$I_D = k \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$ (resistive regime)

Note 1: we use k , many others β , but $k = \beta$

Note 2: resistive regime a.k.a. triode regime

Storey uses $K = 1/k$

Storey: Ohmic region

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I-V Relation

This and similar graphs to follow are from the book

$L_D = 10 \mu m$, $W = 15 \mu m$

Quadratic dependence

$I_D = k \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$ (resistive regime)

This formula only valid in resistive regime. This corresponds to the region to the left of the $V_{DS} = V_{GS} - V_T$ curve. There is another regime called 'saturation'. See following slides.

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I-V Relation

This curve is where I_D curves begin to run flat: I_D does not anymore depend on V_{DS}

$I_D = k \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$

The curve is given by $\frac{dI_D}{dV_{DS}} = k \left[(V_{GS} - V_T) - V_{DS} \right] = 0 \Rightarrow V_{DS} = V_{GS} - V_T$

The value $V_{DS} = V_{GS} - V_T$ is special: it is the boundary between resistive regime and saturation regime (pinch-off)

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Transistor in Saturation

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I-V in saturation

$V_{DS} < V_{GS} - V_T$

$I_D = k \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$

Saturation: $V_{DS} > V_{GS} - V_T$

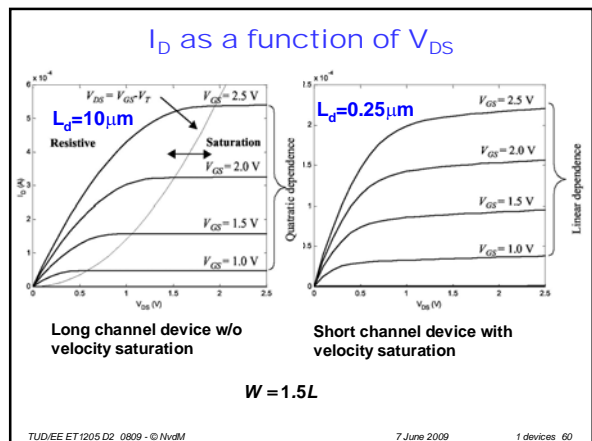
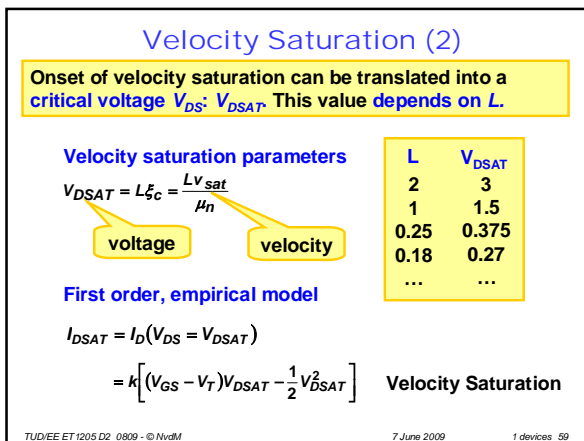
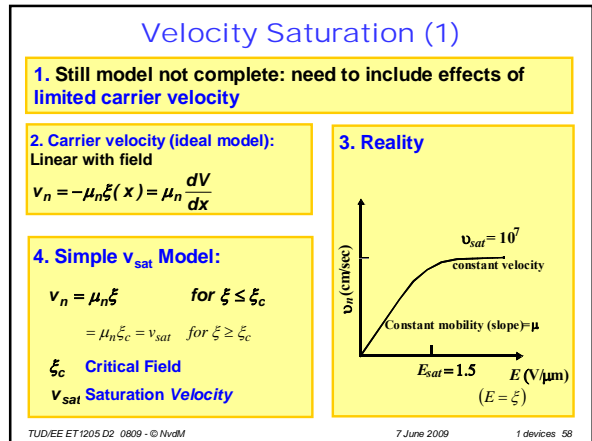
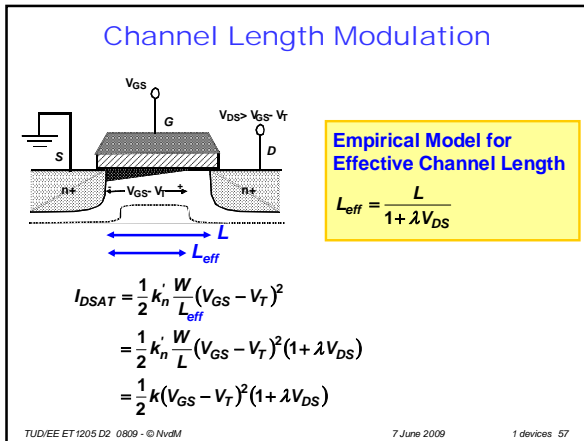
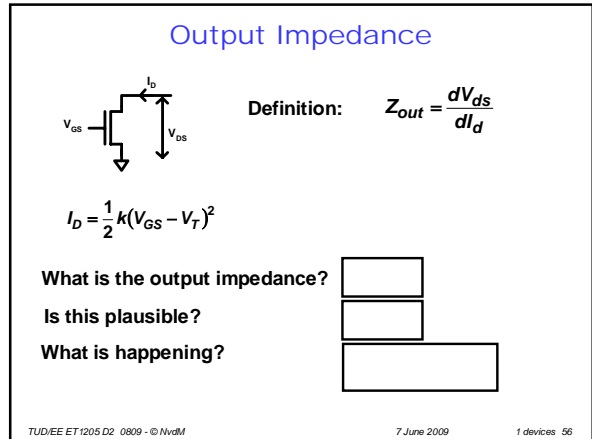
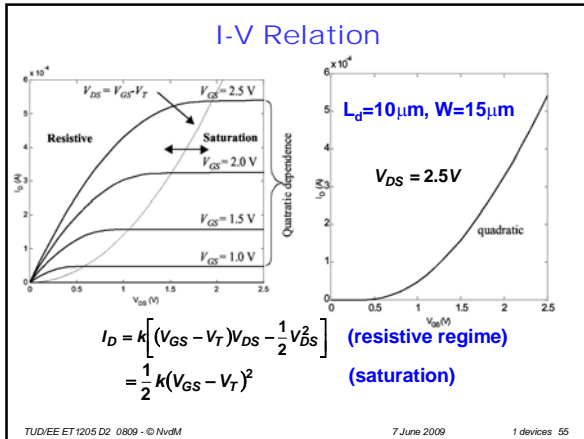
Current does not increase when $V_{DS} > V_{GS} - V_T$

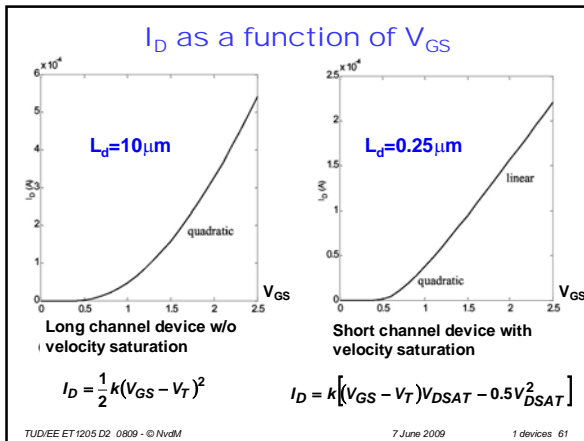
$I_{DSAT} = I_D \Big|_{V_{DS} = V_{GS} - V_T}$ **Saturation current**

$I_{DSAT} = k \left[(V_{GS} - V_T) (V_{GS} - V_T) - \frac{1}{2} (V_{GS} - V_T)^2 \right]$

$= \frac{1}{2} k (V_{GS} - V_T)^2$

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Overview

$$i_D = \begin{cases} k [(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2] & \text{resistive regime} \\ \frac{1}{2} k (V_{GS} - V_T)^2 & \text{when } V_{DS} > V_{GS} - V_T: \text{ saturation} \\ k [(V_{GS} - V_T) V_{DSAT} - \frac{1}{2} V_{DSAT}^2] & \text{when } V_{DS} > V_{DSAT}: \text{ velocity saturation} \end{cases}$$

base equation
replace V_{DS} by V_{GS}-V_T in base equation
replace V_{DS} by V_{DSAT} in base equation

$I_D = I_D' (1 + \lambda V_{DS})$ Channel Length Modulation

Smallest of V_{DS}, V_{GS}-V_T, V_{DSAT} determines operating region

- Velocity saturation
- Saturation
- Resistive

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MOS Models for Manual Analysis

Channel length modulation added to resistive region, in order to enforce continuity

Region Specific Models

$I_D' = k (V_{GT} V_{DS} - 0.5 V_{DS}^2)$ Resistive region

$I_D' = k (V_{GT} V_{GT} - 0.5 V_{GT}^2)$ Saturation

$I_D' = k (V_{GT} V_{DSAT} - 0.5 V_{DSAT}^2)$ Velocity Saturation

$I_D = I_D' (1 + \lambda V_{DS})$ Channel Length Modulation

Comprehensive model

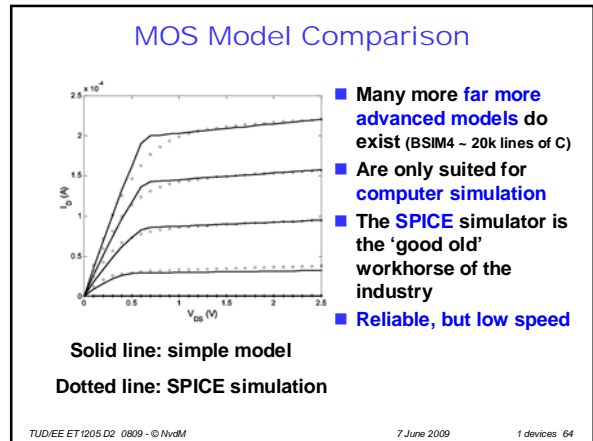
$I_D = k (V_{GT} V_{MIN} - 0.5 V_{MIN}^2) (1 + \lambda V_{DS})$ for $V_{GT} \geq 0$

$= 0$ for $V_{GT} \leq 0$

$V_{MIN} = \text{MIN}(V_{DS}, V_{GT}, V_{DSAT})$

$V_{GT} = V_{GS} - V_T, \quad V_T = V_{T0} + \gamma (\sqrt{|-2\phi_F + V_{SB}|} - \sqrt{|-2\phi_F|})$

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NMOS vs. PMOS

- PMOS (V_{DS}, V_{GS}, I_D, V_T) < 0
- Can calculate as if NMOS using absolute values
- PMOS device not as strong as NMOS

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NMOS vs. PMOS (2)

Zero-field mobility (bulk!) Velocity vs. Field

$\mu_p < \mu_n \Rightarrow k_p < k_n$

$v_{sat_p} \approx v_{sat_n} \Rightarrow |V_{DSAT_p}| > |V_{DSAT_n}|$

	V _{th} (V)	γ (V ^{0.5})	V _{DSAT} (V)	k' (A/V ²)	λ (V ⁻¹)
NMOS	0.43	0.4	0.63	115 × 10 ⁻⁹	0.06
PMOS	-0.4	-0.4	-1	-30 × 10 ⁻⁹	-0.1

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Alternative Saturation Expression

- Saturation if $V_{DS} > V_{GS} - V_T$
- Show that $V_{DS} > V_{GS} - V_T \Leftrightarrow V_{GD} < V_T$
- Proof:
 - $V_{DS} > V_{GS} - V_T$
 - $\Leftrightarrow V_D - V_S > V_G - V_S - V_T$
 - $\Leftrightarrow V_D > V_G - V_T$
 - $\Leftrightarrow V_G - V_T < V_D$
 - $\Leftrightarrow V_G - V_D < V_T$
 - $\Leftrightarrow V_{GD} < V_T$

Physically this relates to 'amount of inversion' at drain side
If inversion at drain side disappears: pinch-off

- This is an alternative expression for the saturation region
- Can be handy

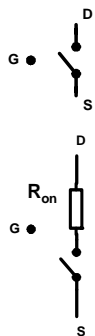
MOS Device Symmetry

- MOS transistors are **symmetrical**
- Strong inversion at source if $V_{GS} > V_T$
- Strong inversion at drain if $V_{GD} > V_T$
- You should check the I-V relations when interchanging drain and source
- Identification of source drain only by **convention**
- Determined by circuit-environment

	NMOS	PMOS	General
Source	V_{SS} -side	V_{DD} -side	Strongest inversion
Drain	V_{DD} -side	V_{SS} -side	Weakest inversion

V_{SS} : low supply voltage, V_{DD} = high supply voltage

Improved MOS Transistor Switch Level Model



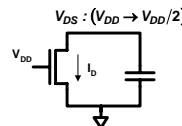
Position of switch depends on gate to source voltage

V_{GS}	NMOS	PMOS
hi	closed	open
lo	open	closed

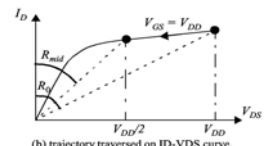
More detailed model may include R_{on}

- R_{on} is highly non-linear
- Make linear approximation R_{eq}
- Model with (linear) R_{eq} less detailed then previous equation based model, but often useful for first estimates of behavior

Switch Model R_{on}



(a) Schematic



(b) trajectory traversed on ID-VDS curve.

$$R_{eq} = \frac{1}{2} \left[\frac{V_{DD}}{I_{DSAT} (1 + \lambda V_{DD})} + \frac{V_{DD}/2}{I_{DSAT} (1 + \lambda V_{DD}/2)} \right]$$

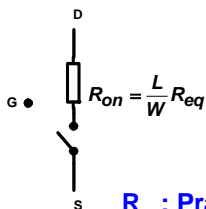
$$\frac{1}{1 + \lambda V_{DD}} \approx 1 - \lambda V_{DD} + \mathcal{O}(\lambda^2 V_{DD}^2) \quad \text{2.3\% error with } \lambda = 0.06 \text{ V}^{-1}, V_{DD} = 2.5 \text{ V}$$

$$R_{eq} \approx \frac{1}{2} \frac{V_{DD}}{I_{DSAT}} \left[1 - \lambda V_{DD} + \frac{1}{2} (1 - \lambda V_{DD}/2) \right]$$

$$= \frac{3}{4} \frac{V_{DD}}{I_{DSAT}} \left[1 - \frac{5}{6} \lambda V_{DD} \right]$$

Theory!

MOS Transistor Switch Level Model (Empirical).



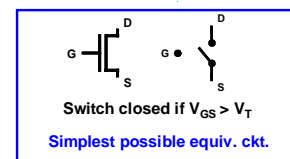
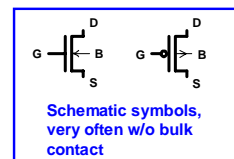
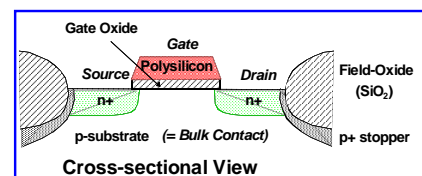
Position of switch depends on gate to source voltage

V_{GS}	NMOS	PMOS
hi	closed	open
lo	open	closed

R_{eq} : Practice!

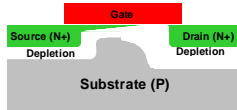
$R_{eq} \setminus V_{gd} \text{ (V)}$	1	1.5	2	2.5
NMOS (k Ω)	35	19	15	13
PMOS (k Ω)	115	55	38	31

The MOS Transistor Summary



The MOS Transistor Summary ctd.

- Need to **analyze** speed, power, noise etc of MOS circuits
- Simple switch-level model **not sufficient**
- Study exact operation to derive **more precise IV relations**



$$I_D = k(V_{GT}V_{MIN} - 0.5V_{MIN}^2)(1 + \lambda V_{DS}) \quad \text{for } V_{GT} \geq 0$$

$$= 0 \quad \text{for } V_{GT} \leq 0$$

$$V_{MIN} = \text{MIN}(V_{DS}, V_{GT}, V_{DSAT})$$

$$V_{GT} = V_{GS} - V_T, \quad V_T = V_{T0} + \gamma(\sqrt{|-2\phi_F + V_{SB}|} - \sqrt{-2\phi_F})$$

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Summary

- Semiconductor Physics
- The diode
 - Depletion, I-V relations, capacitance, secondary effects, models
- The MOS transistor
 - First glance, threshold, I-V relations, models
 - Dynamic behavior (capacitances), resistances, more Second-Order effects, models

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