Perception and Binaural Signal Processing

EE4715 Array Processing | 7 June '24



Audio Signal Processing Applications













MVDR Beamforming

- STFT domain (short-time stationarity assumption)
- narrowband assumption
- minimise output noise power
- target preservation constraint

$$\boldsymbol{x}(k,l) = \boldsymbol{a}(k,l)s(k,l) + \boldsymbol{n}(k,l)$$

$$y(k,l) = \boldsymbol{w}^{\mathrm{H}}(k,l)\boldsymbol{x}(k,l)$$

minimise
$$\boldsymbol{w}^{\mathrm{H}}(k,l)\boldsymbol{R}_{\boldsymbol{n}}(k,l)\boldsymbol{w}(k,l)$$

subject to $\boldsymbol{w}^{\mathrm{H}}(k,l)\boldsymbol{a}(k,l)=1$

$$oldsymbol{w}(k,l) = rac{oldsymbol{R}_{oldsymbol{n}}^{-1}(k,l)oldsymbol{a}(k,l)}{oldsymbol{a}^{ ext{H}}(k,l)oldsymbol{R}_{oldsymbol{n}}^{-1}(k,l)oldsymbol{a}(k,l)}$$



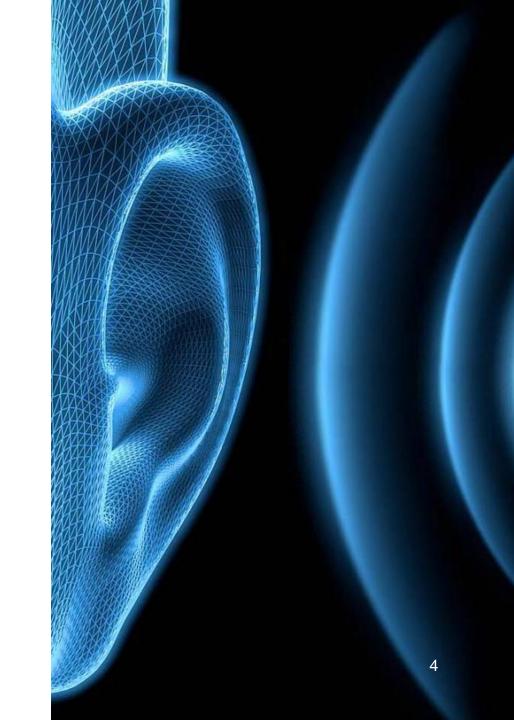
Speech Intelligibility in Noise

'Measure of how comprehensible speech is in given conditions'

Factors that influence speech intelligibility:

- energetic masking
- informational masking
- attention/listening effort
- cognitive abilities/language proficiency
- hearing impairment
- reverberation
- spatial distribution (auditory stream segregation)





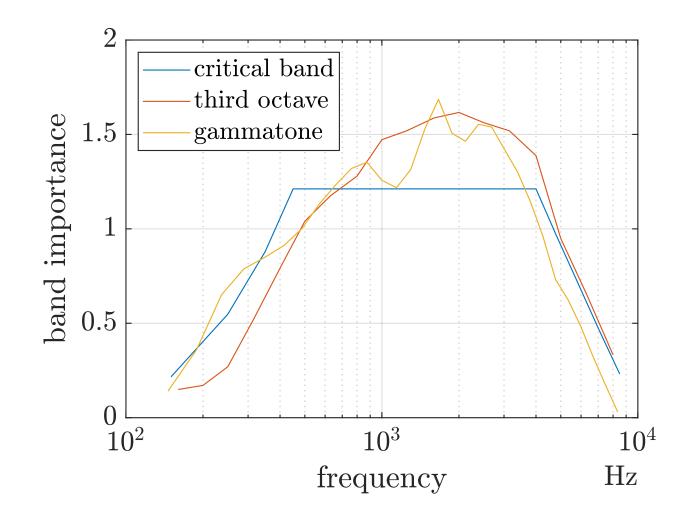


Measuring Intelligibility

- matrix test
- speech reception threshold (SRT)
- audiogram

Speech Intelligibility Index (SII)

- objective measure, ANSI standard
- started as articulation index (AI), 1947
- filter speech and noise into frequency bands
- perceptually weighted average of band SNRs
- convert weighted average SNR to intelligibility score

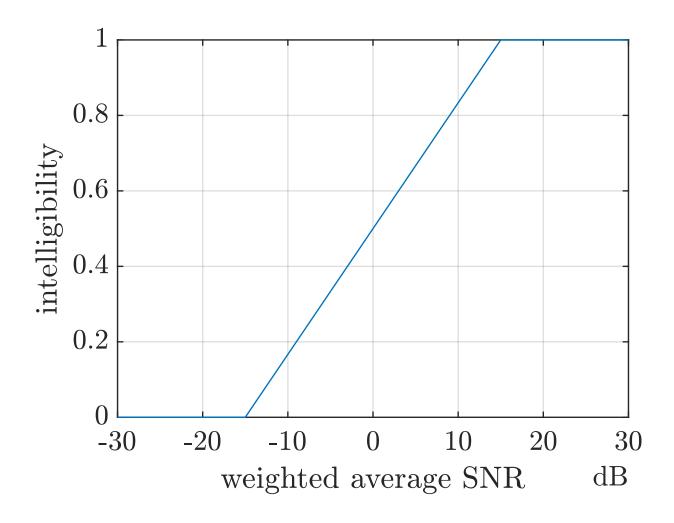




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- objective measure, ANSI standard
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- filter speech and noise into frequency bands
- perceptually weighted average of band SNRs
- convert weighted average SNR to intelligibility score
- internal noise to model hearing thresholds
- SRT measure

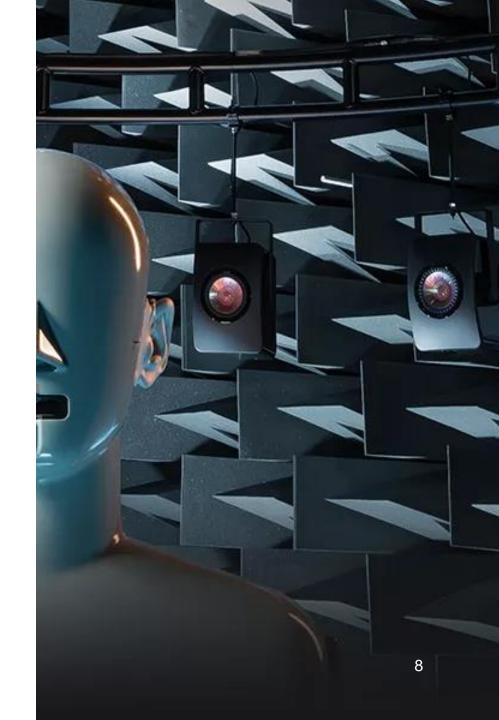




Other Intelligibility Measures

- speech transmission index (STI)
- coherence speech intelligibility index (CSII)
- short-time objective intelligibility (STOI)
- hearing-aid speech perception index (HASPI)
- data-driven measures





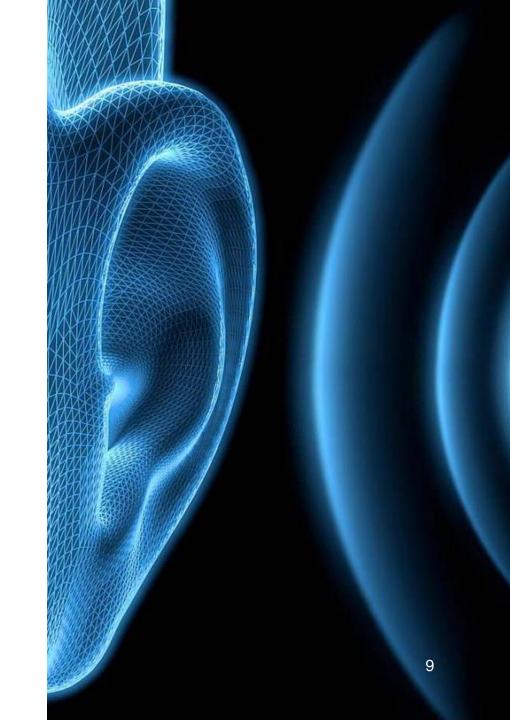
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Spatial Release from Masking

two main binaural cues:

- interaural time difference (ITD) mainly < 1000 Hz
- interaural level difference (ILD) mainly > 1500 Hz

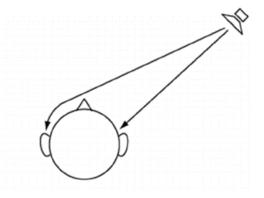
interaural transfer function (ITF)

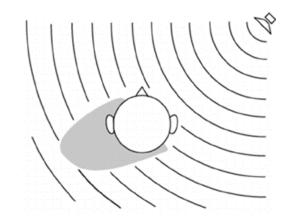
binaural cue consistency across frequency

$$ITF = \frac{a_{\rm L}}{a_{\rm R}}$$

$$ITD = \frac{\angle ITF}{\omega} = \frac{\angle ITF}{2\pi f}$$

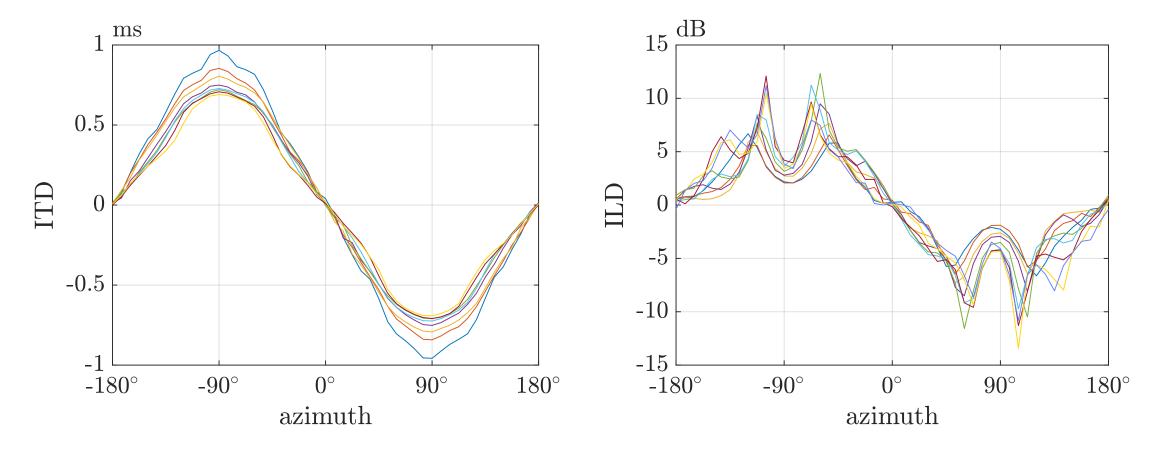
$$ILD = |ITF|$$





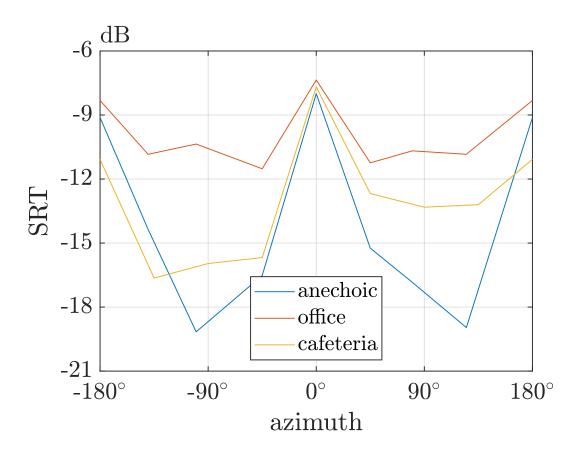


Spatial Release from Masking





Spatial Release from Masking





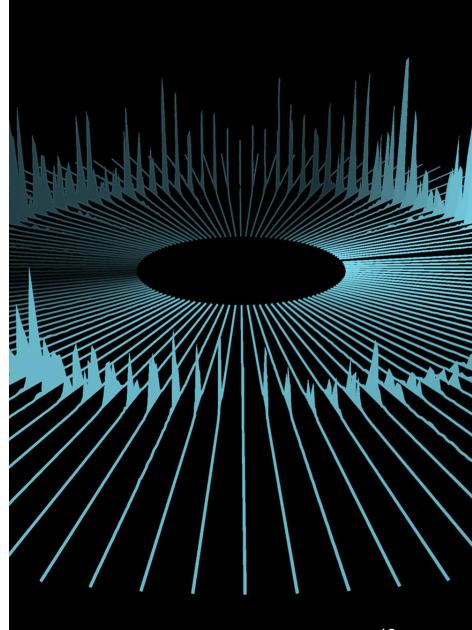
Binaural Intelligibility Models

information used:

- SNR (energy)
- modulation
- correlation
- glimpsing

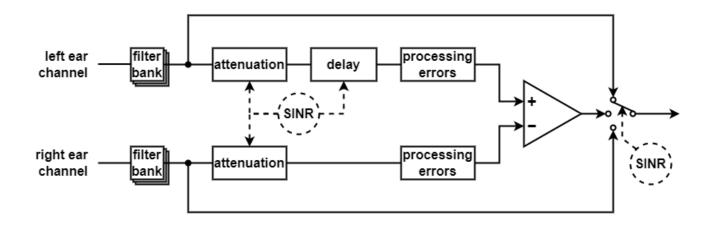
input availability (blindness, intrusiveness)
offline/real time
physiological interpretability





Binaural Speech Intelligibility Model

- 1. gammatone filter bank
- 2. internal masking noise
- 3. equalisation—cancellation (Durlach, 1963)
- 4. artificial processing errors
- 5. better ear listening
- 6. monaural intelligibility measure (SII)





Binaural Speech Intelligibility Model

$$y_{\rm EC}(t) = e^{\frac{1}{2}\gamma} y_{\rm L}(t + \frac{1}{2}\tau) - e^{-\frac{1}{2}\gamma} y_{\rm R}(t - \frac{1}{2}\tau)$$

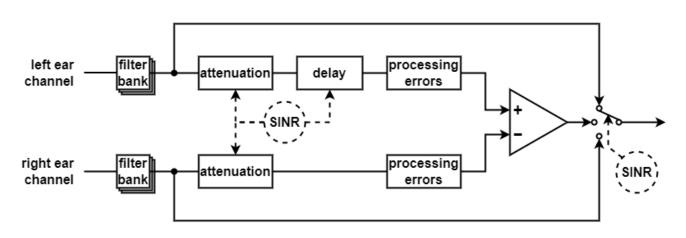
$$y_{\rm EC}(\omega) = e^{\frac{1}{2}(\gamma + j\omega\tau)} y_{\rm L}(\omega) - e^{-\frac{1}{2}(\gamma + j\omega\tau)} y_{\rm R}(\omega)$$

$$oldsymbol{y} = egin{pmatrix} y_{
m L} \ y_{
m R} \end{pmatrix} \qquad oldsymbol{v} = egin{pmatrix} {
m e}^{rac{1}{2}(\gamma-j\omega au)} \ {
m -e}^{-rac{1}{2}(\gamma-j\omega au)} \end{pmatrix}$$

$$ext{SNIR}(y_{ ext{EC}}) = rac{oldsymbol{v}^{ ext{H}} oldsymbol{P_s} oldsymbol{v}}{oldsymbol{v}^{ ext{H}} oldsymbol{P_n} oldsymbol{v}}$$

$$y_{
m EC} = oldsymbol{v}^{
m H} oldsymbol{y}$$

$$\boldsymbol{P_y} = \int \mathrm{E}\left(\boldsymbol{y}\boldsymbol{y}^{\mathrm{H}}\right) d\omega$$





Binaural MVDR

binaural signal model

reference transfer function constraint

What happens to the binaural cues?

- Target binaural cues are preserved.
- Noise sources virtually move to target!

$$\left\{egin{aligned} oldsymbol{x} &= oldsymbol{a}s + oldsymbol{n}_0 + \sum_i oldsymbol{b}_i n_i \ y_{
m L} &= oldsymbol{w}_{
m L}^{
m H} oldsymbol{x} \ y_{
m R} &= oldsymbol{w}_{
m R}^{
m H} oldsymbol{x} \end{aligned}
ight.$$

minimise
$$\boldsymbol{w}_{\mathrm{L}}^{\mathrm{H}}\boldsymbol{R}_{\boldsymbol{n}}\boldsymbol{w}_{\mathrm{L}}$$
subject to $\boldsymbol{w}_{\mathrm{L}}^{\mathrm{H}}\boldsymbol{a}=a_{\mathrm{L}}$
 $\boldsymbol{w}_{\mathrm{L}}=\frac{\boldsymbol{R}_{\boldsymbol{n}}^{-1}\boldsymbol{a}}{\boldsymbol{a}^{\mathrm{H}}\boldsymbol{R}_{\boldsymbol{n}}^{-1}\boldsymbol{a}}a_{\mathrm{L}}^{*}$

$$\text{ITF}_{\text{out}}(s) = \frac{\boldsymbol{w}_{\text{L}}^{\text{H}}\boldsymbol{a}}{\boldsymbol{w}_{\text{R}}^{\text{H}}\boldsymbol{a}} = \frac{a_{\text{L}}}{a_{\text{R}}} = \text{ITF}(s)$$

$$\text{ITF}_{\text{out}}(n_i) = \frac{\boldsymbol{w}_{\text{L}}^{\text{H}} \boldsymbol{b}_i}{\boldsymbol{w}_{\text{R}}^{\text{H}} \boldsymbol{b}_i} = \frac{a_{\text{L}}}{a_{\text{R}}} = \text{ITF}(s)$$



Joint Binaural LCMV

add binaural cue preservation constraint(s)

couple left and right problems

closed-form solution exists

reduced degrees of freedom for SNR maximisation!

$$\left\{egin{aligned} oldsymbol{x} &= oldsymbol{a}s + oldsymbol{n}_0 + \sum_i oldsymbol{b}_i n_i \ y_{
m L} &= oldsymbol{w}_{
m L}^{
m H} oldsymbol{x} \ y_{
m R} &= oldsymbol{w}_{
m R}^{
m H} oldsymbol{x} \end{aligned}
ight.$$

$$rac{oldsymbol{w}_{
m L}^{
m H}oldsymbol{b}_i}{oldsymbol{w}_{
m R}^{
m H}oldsymbol{b}_i} = rac{b_{i
m L}}{b_{i
m R}} \quad \Leftrightarrow \quad oldsymbol{w}_{
m L}^{
m H}oldsymbol{b}_ib_{i
m R} = oldsymbol{w}_{
m R}^{
m H}oldsymbol{b}_ib_{i
m L}$$

$$egin{aligned} & \mathbf{minimise} \ \mathbf{w}_{
m L}^{
m H} oldsymbol{R}_{oldsymbol{n}} \mathbf{w}_{
m L} + oldsymbol{w}_{
m R}^{
m H} oldsymbol{R}_{oldsymbol{n}} \mathbf{w}_{
m R} \end{aligned} egin{aligned} & \mathbf{w}_{
m L}^{
m H} oldsymbol{a} = a_{
m L}, \ & \mathbf{w}_{
m R}^{
m H} oldsymbol{a} = a_{
m R}, \ & \mathbf{w}_{
m L}^{
m H} oldsymbol{b}_i b_{i
m R} = oldsymbol{w}_{
m R}^{
m H} oldsymbol{b}_i b_{i
m L} \end{aligned}$$



Perception-Based Beamformer

- include BSIM to account for SRM
- maximise 'perceived' SNR

Binaural MVDR is one of the solutions!

$$\left\{egin{aligned} oldsymbol{x} &= oldsymbol{a} s + oldsymbol{n}_0 + \sum_i oldsymbol{b}_i n_i \ oldsymbol{y} &= oldsymbol{W}^{\mathrm{H}} oldsymbol{x} = \left(oldsymbol{w}_{\mathrm{L}} \quad oldsymbol{w}_{\mathrm{R}}
ight)^{\mathrm{H}} oldsymbol{x} \ z = oldsymbol{v}^{\mathrm{H}} oldsymbol{y} \end{array}
ight.$$

$$egin{array}{ll} ext{maximise} & rac{m{v}^{ ext{H}}m{W}^{ ext{H}}m{a}m{a}^{ ext{H}}m{W}m{v}}{m{v}^{ ext{H}}m{W}^{ ext{H}}m{R}_{m{n}}m{W}m{v}} \ ext{subject to} & m{W}^{ ext{H}}m{a} = m{a}_{ ext{ref}} \ \end{array}$$



TUDelft